



TEXAS A&M UNIVERSITY

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Vehicular Teamwork: Collaborative Localization of Autonomous Vehicles

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IEEE International Conference on Intelligent Transportation 2021

Presentation Outline

- Motivation
- Introduction
 - Ultra-Wideband Technology
- Theory
 - Decentralized Collaborative Localization
- Results
 - Simulated
 - Experimental
- Conclusions

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Autonomous Vehicles



Sardari, LoKan, 2014, "Google self-driving car" [6]

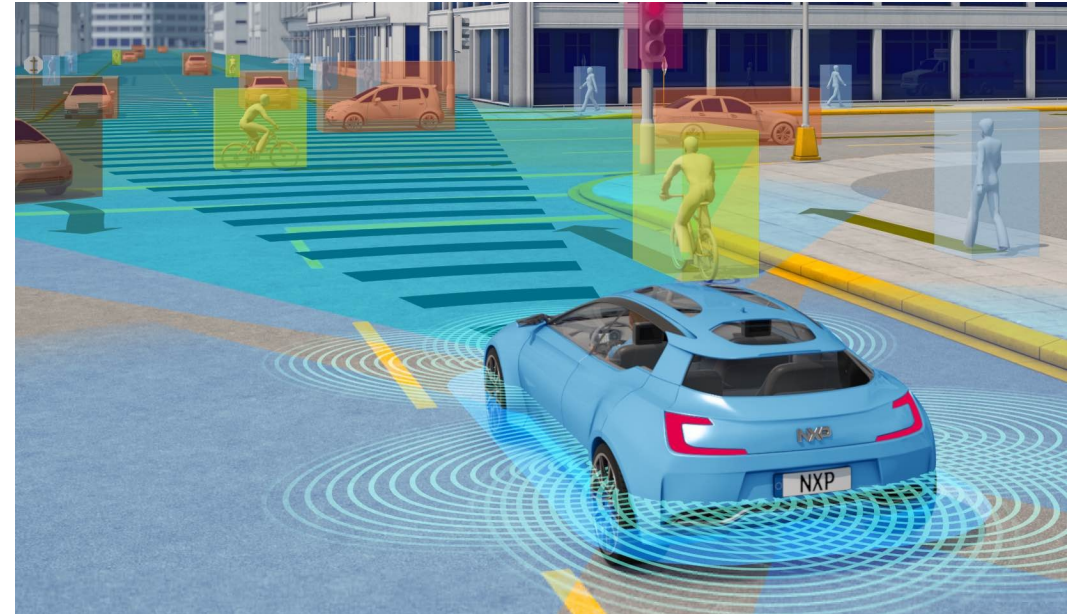
AV Sensors

Perception

- Radar
- Lidar
- Cameras
- Ultra Sonic

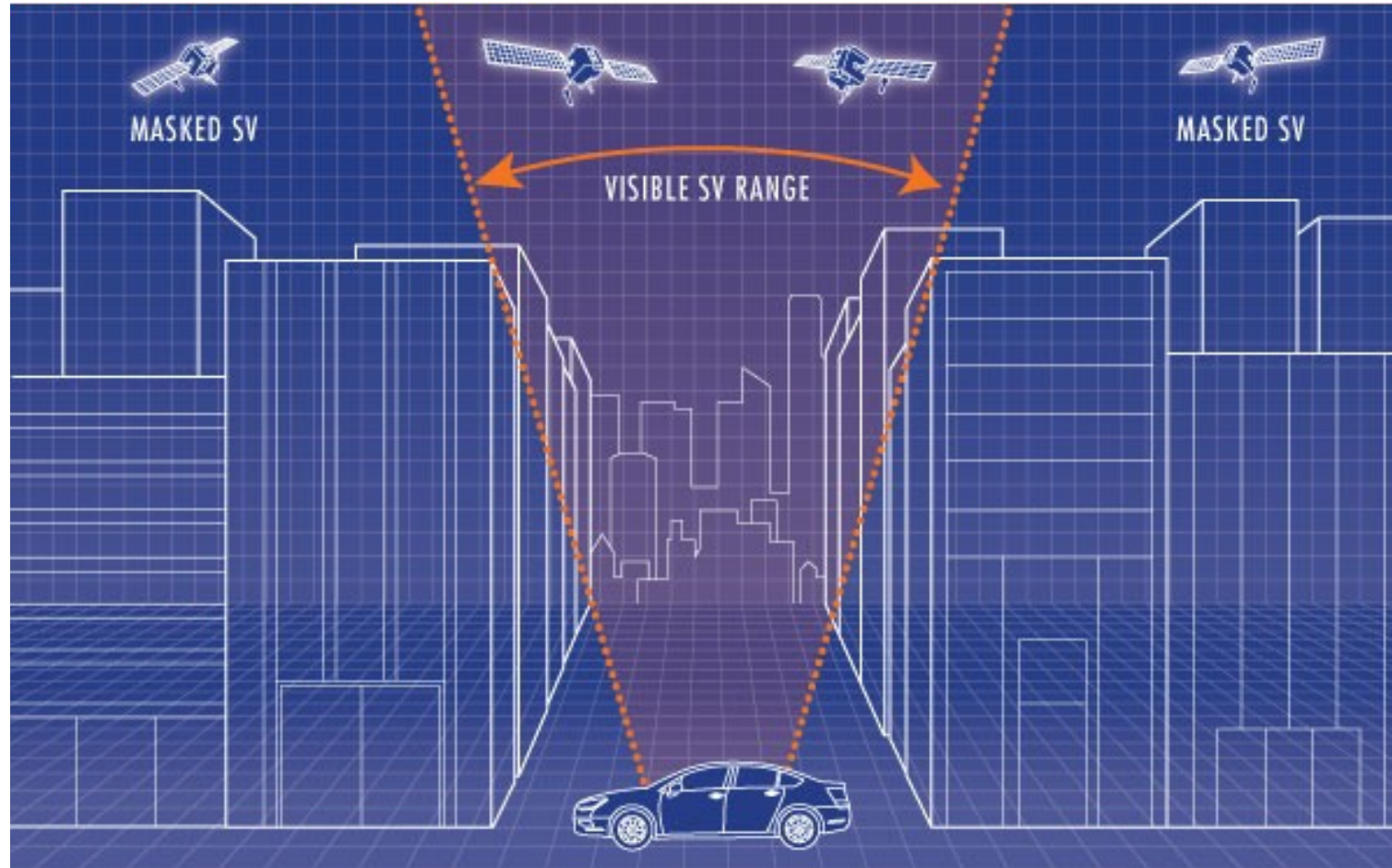
Localization

- Inertial Measurement Unit (IMU)
- Wheel and Steering Odometry
- Global Navigation Satellite System (GNSS)



Electronics Weekly, 2017, CES Autonomous cars and the sensors to make them safe [9]

Urban Canyons



Kumar, Muthukumar, 2014, *GNSS Shadow Matching: Improving GNSS positioning in Urban Canyons* [10]

AV Limitations

Difficulty in transitioning to GPS-denied environments



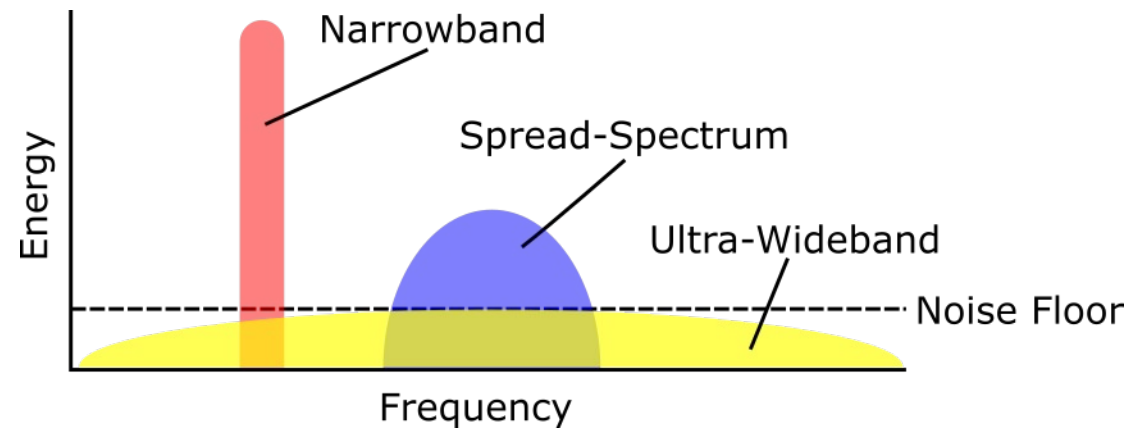
iDigHardware, 2017, *Decoded: Securing Parking Garages* [11]

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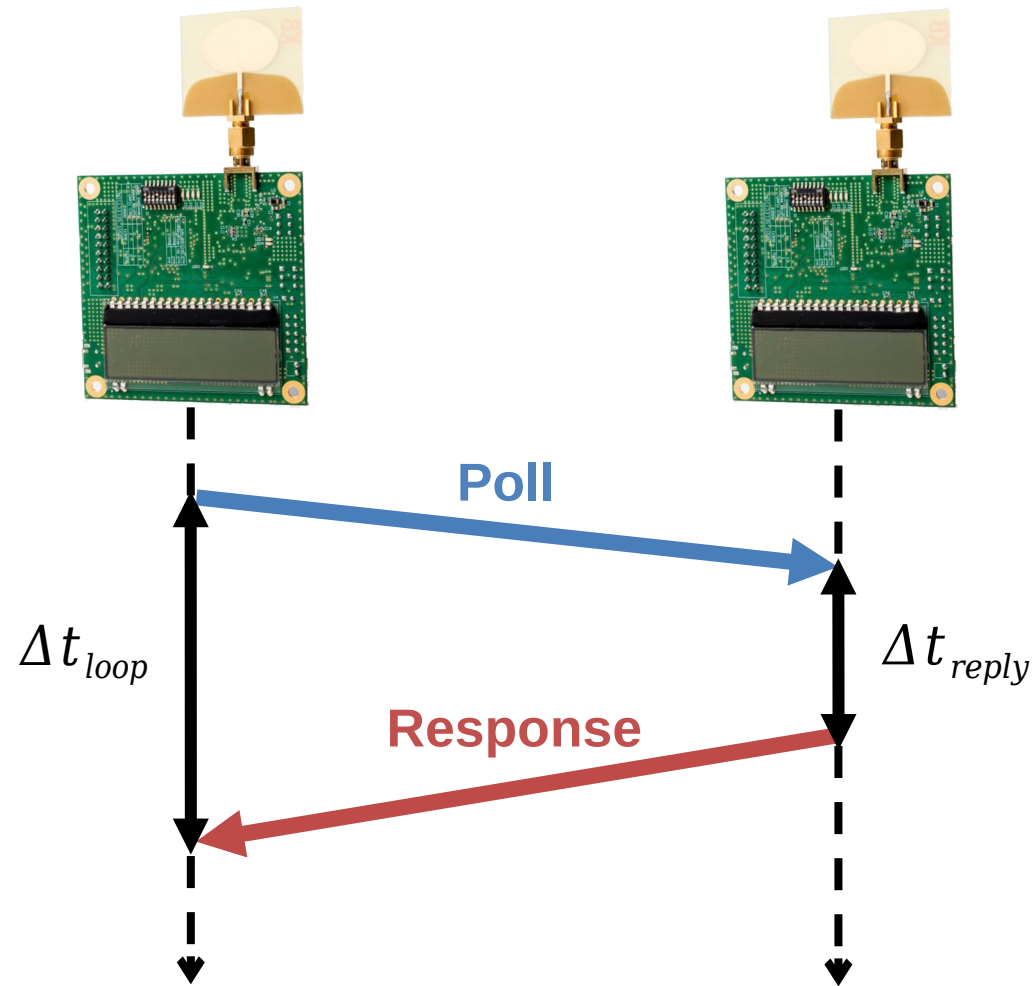
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Ultra-Wideband Technology

- FCC first regulated in 2002 [1]
- Large Bandwidth (>500 MHz) Low Power Radio
- Pulses occupy entire UWB bandwidth
- Shared Spectrum
- Relative immunity to multipath errors



UWB Ranging



$$TimeofFlight = \frac{\Delta t_{loop} - \Delta t_{reply}}{2}$$

$$Distance = \frac{TimeofFlight}{c}$$

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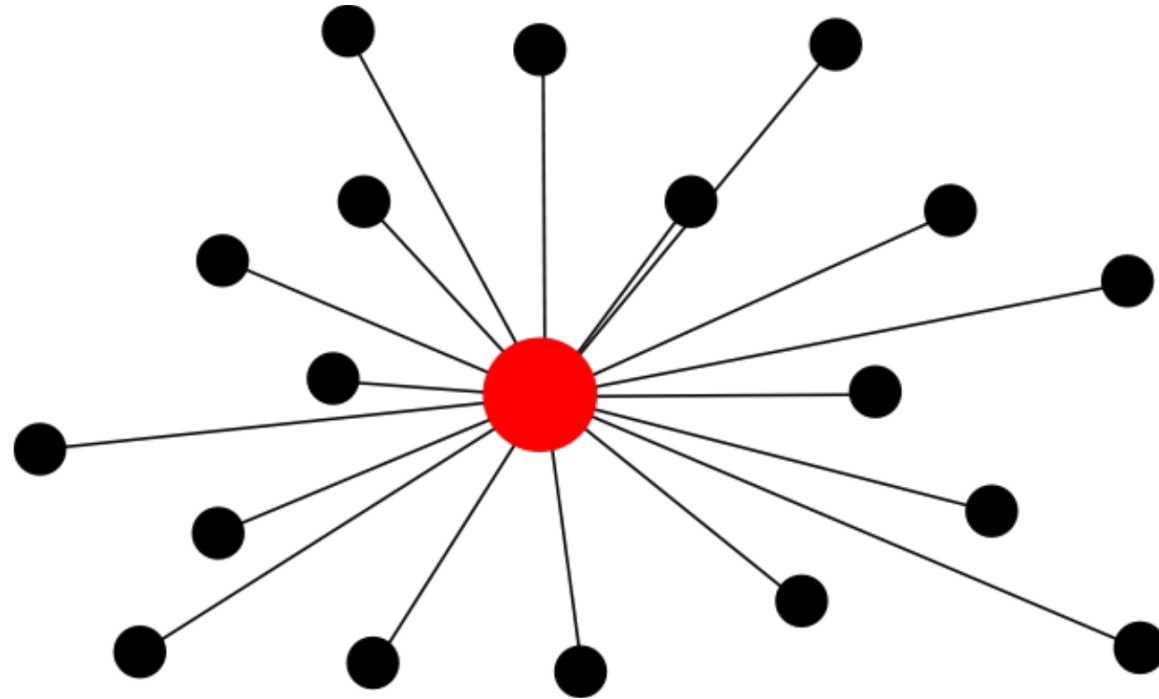
Collaborative Localization



"Traffic jam" by [lynac](#) is licensed under [CC BY-NC 2.0](#) [16]

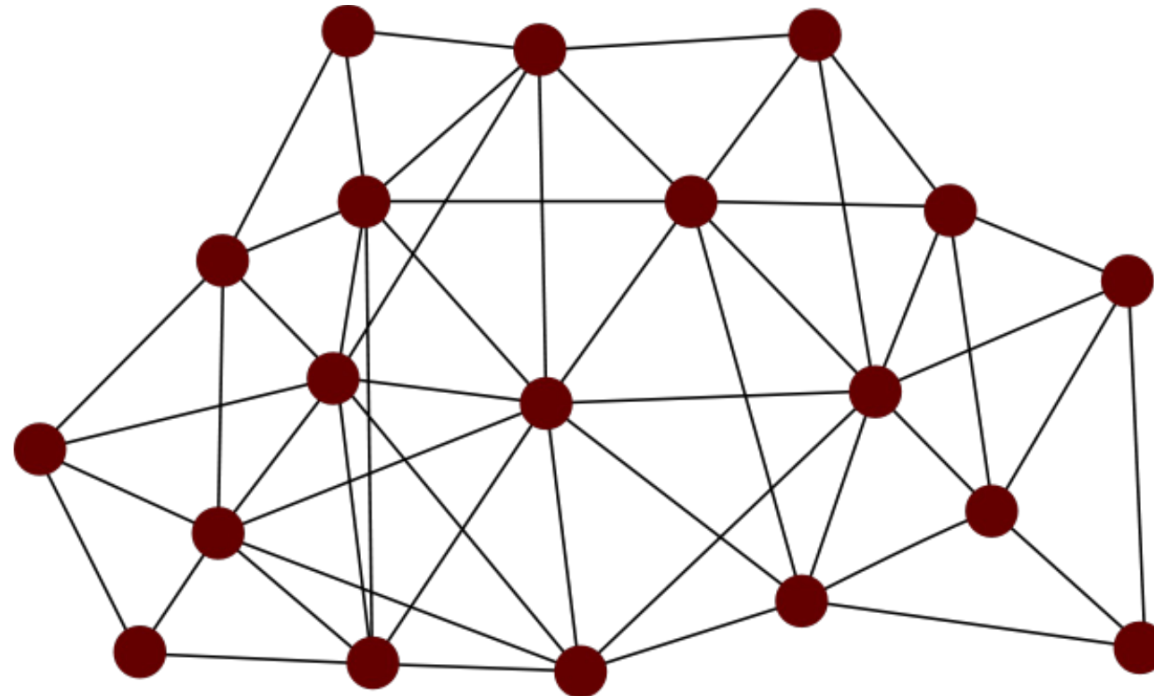
Collaborative Localization

- Centralized:



Collaborative Localization

- Decentralized



Kalman Filter

- Linear Quadratic Estimation
- Recursive Two-Step Process
 - Prediction step
 - Update step
- Commonly used for guidance and control problems
- Nonlinear measurement and process models
 - Linearized to form Extended Kalman Filter

DCL Algorithm

- Distributed Approximation of Extended Kalman Filter
- Derived by *Luft, L. et. al.* [4]
- Recursive Three-Step Process
 - Control (Prediction) Step
 - Private Update Step
 - Relative Update Step
- Number of relative nodes varies with time

DCL Algorithm

Joint State:

$$\hat{x}^t = [\hat{x}_1^t; \dots; \hat{x}_N^t]$$

$$\Sigma^t = [\Sigma_{ij}^t]_{1 \leq i, j \leq N}$$

Initialization:

$$\hat{x}^0 = [\hat{x}_1^0; \dots; \hat{x}_N^0]$$

$$\Sigma^0 = \begin{bmatrix} \Sigma_{11}^0 & & 0 \\ & \ddots & \\ 0 & & \Sigma_{NN}^0 \end{bmatrix}$$

Decomposition:

$$\Sigma_{ij}^{t+1} = \sigma_{ij}^{t+1} (\sigma_{ji}^{t+1})^T$$

$$\sigma_{ij}^{t+1} = \Sigma_{ij}^{t+1}$$

$$\sigma_{ji}^{t+1} = I$$

DCL Algorithm

Control Step (Prediction)

EKF

$$\hat{x}^{t+1} = g(\hat{x}^t, u^t)$$

$$P^{t+1} = G^t P^t (G^t)^T + R^t$$

DCL

$$\hat{x}_i^{t+1} = g(\hat{x}_i^t, U_i^t)$$

$$\left\{ \begin{array}{l} \Sigma_{ii}^{t+1} = G_i^t \Sigma_{ii}^t (G_i^t)^T + R_i^t \\ \sigma_{ij}^{t+1} = G \sigma_{ij}^t \end{array} \right.$$

DCL Algorithm

Private Update

EKF

$$S^t = H^t \Sigma^t (H^t)^T + Q^t$$

$$K^t = \Sigma^t (H^t)^T S^{-1}$$

$$\hat{x}^{t+1} = \hat{x}^t + K^t (z^t - h(\hat{x}^t))$$

$$\Sigma^{t+1} = (I - K^t H^t) \Sigma^t$$

for Car i , $j \in \{1, \dots, N\} \setminus \{i\}$

DCL

$$S = H_i^t \Sigma_{ii}^t (H_i^t)^T + Q_i^t$$

$$K_i^t = \Sigma_{ii}^t (H_i^t)^T S^{-1}$$

$$\hat{x}_i^{t+1} = \hat{x}_i^t + K_i^t [z_i^t - h(\hat{x}_i^t)]$$

$$\Sigma_{ii}^{t+1} = (I - K_i^t H_i^t) \Sigma_{ii}^t$$

$$\sigma_{ij}^{t+1} = (I - K_i^t H_i^t) \sigma_{ij}^t$$

DCL Algorithm

Relative Update

EKF

$$S^t = F^t \Sigma^t (F^t)^T + Q^t$$

$$K^t = \Sigma^t (F^t)^T S^{-1}$$

$$\hat{x}^{t+1} = \hat{x}^t + K^t (z^t - h(\hat{x}^t))$$

for Cars $i, j, k \in \{1, \dots, N\} \setminus \{i, j\}$

DCL

$$\Sigma_{ij/ji}^t = \sigma_{ij/ji}^t (\sigma_{ji/ij}^t)^T$$

$$S = [F_i \quad F_j] \begin{bmatrix} \Sigma_{ii}^t & \Sigma_{ij}^t \\ \Sigma_{ji}^t & \Sigma_{jj}^t \end{bmatrix} \begin{bmatrix} F_i^T \\ F_j^T \end{bmatrix} + Q_{ij}^t$$

$$K = \begin{bmatrix} \Sigma_{ii}^t F_i^T & \Sigma_{ij}^t F_j^T \\ \Sigma_{ji}^t F_j^T & \Sigma_{jj}^t F_i^T \end{bmatrix} S^{-1}$$

$$\hat{x}_{i/j}^{t+1} = \hat{x}_{i/j}^t + K_{i/j} [z_{ij}^t - h(\hat{x}_i^{t+1}, \hat{x}_j^{t+1})]$$

$$F_{i/j}^t = \frac{\partial f(x_i, x_j)}{\partial x_{i/j}} (\hat{x}_{i/j}^t)$$

DCL Algorithm

Relative Update

EKF

$$\Sigma^{t+1} = (I - K^t F^t) \Sigma^t$$

for Cars $i, j, k \in \{1, \dots, N\} \setminus \{i, j\}$

DCL

$$\Sigma_{ii/jj}^{t+1} = (I - K_{i/j} F_{i/j}) \Sigma_{ii/jj}^t - K_{i/j} F_{j/i} \Sigma_{ji/ij}^t$$

$$\Sigma_{ij}^{t+1} = (I - K_i F_i) \Sigma_{ij}^t - K_i F_j \Sigma_{jj}^t$$

$$\sigma_{ij}^{t+1} = \Sigma_{ij}^{t+1}$$

$$\sigma_{ji}^{t+1} = I$$

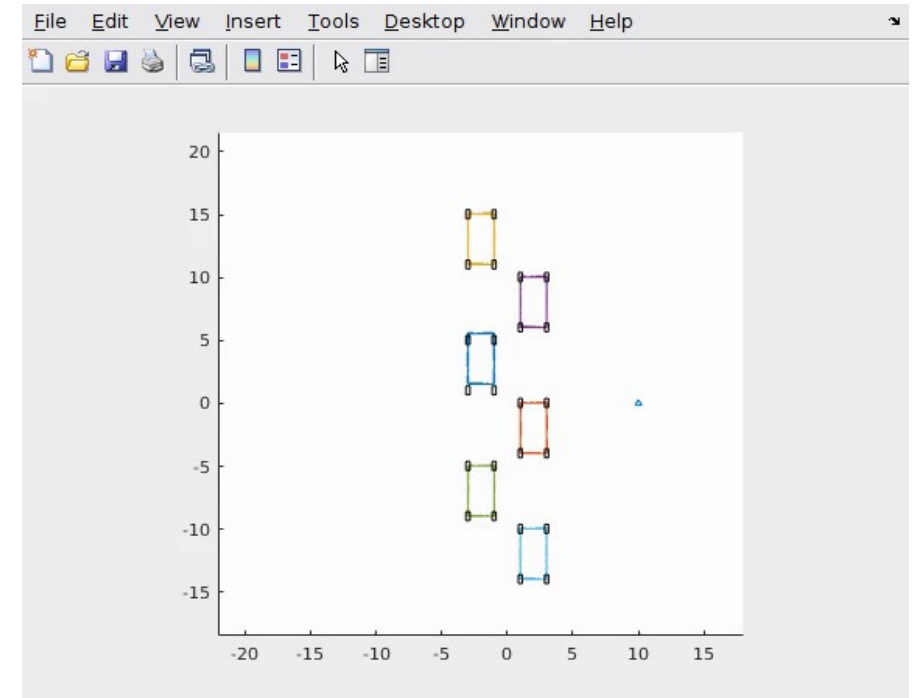
$$\sigma_{ik/jk}^{t+1} = \Sigma_{ii/jj}^{t+1} \left(\Sigma_{ii/jj}^{t+1} \right)^{-1} \sigma_{ik/jk}^t$$

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Simulation Environment

- Models n -vehicles with random sensor errors
- IMU, Odometry, GPS, and UWB
- Handles landmarks and collaboration
- Simulates estimation algorithms
 - Single Vehicle EKF
 - Centralized EKF with UWB
 - Decentralized EKF with UWB
- Programmed in MatLab
- Open Sourced

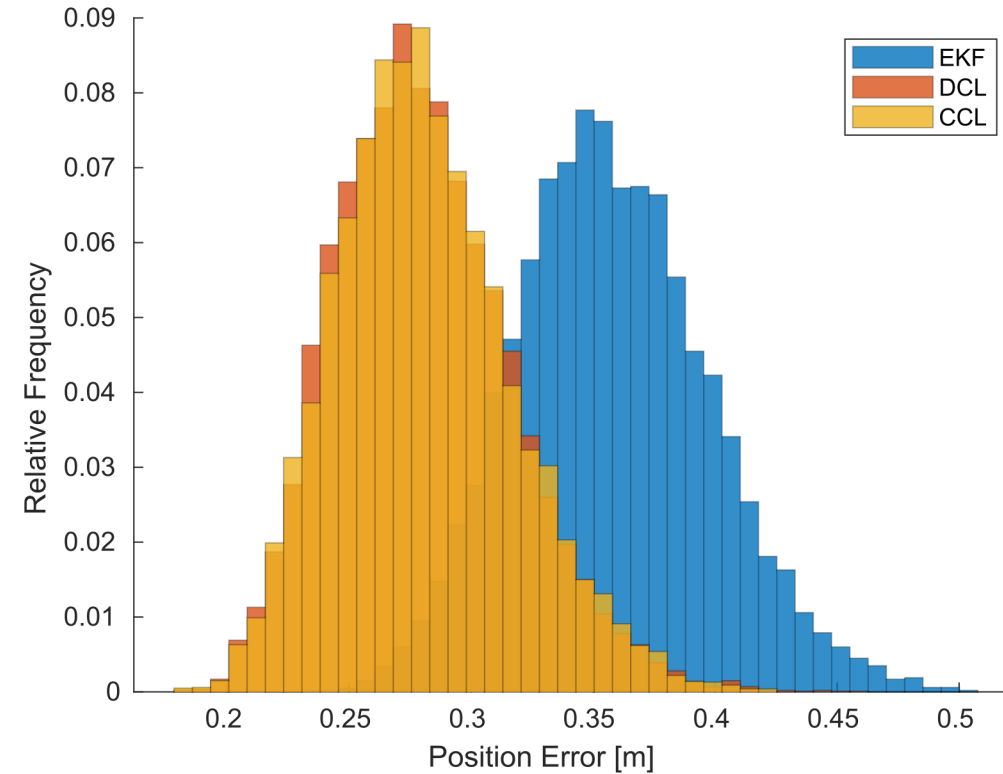
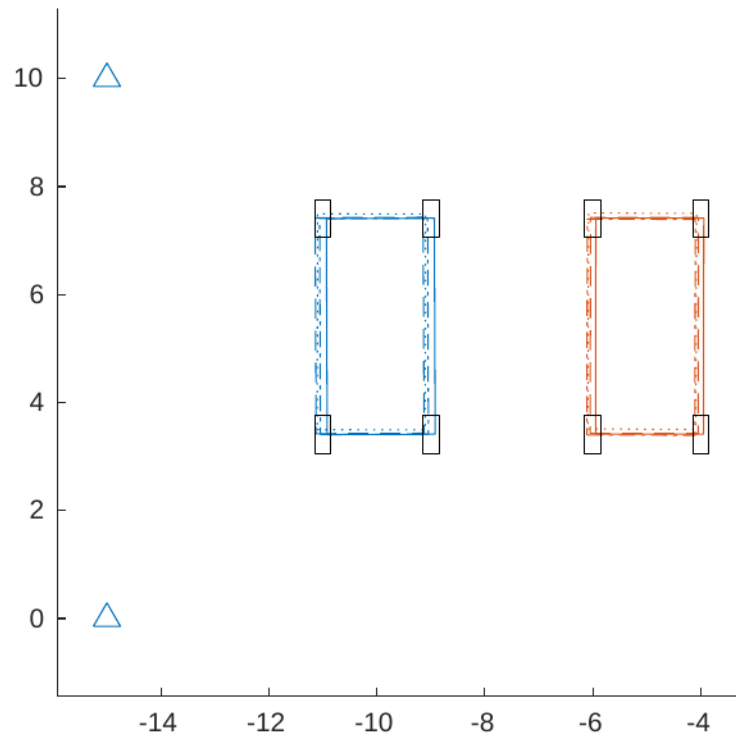


Monte Carlo Simulations

- Monte Carlo Simulation Parameters
 - 10,000 Runs Each
 - Parallelized for faster processing
 - With and Without UWB Landmarks
 - With and Without UWB Collaboration
 - Calculates RMS position error
 - 20 second simulations

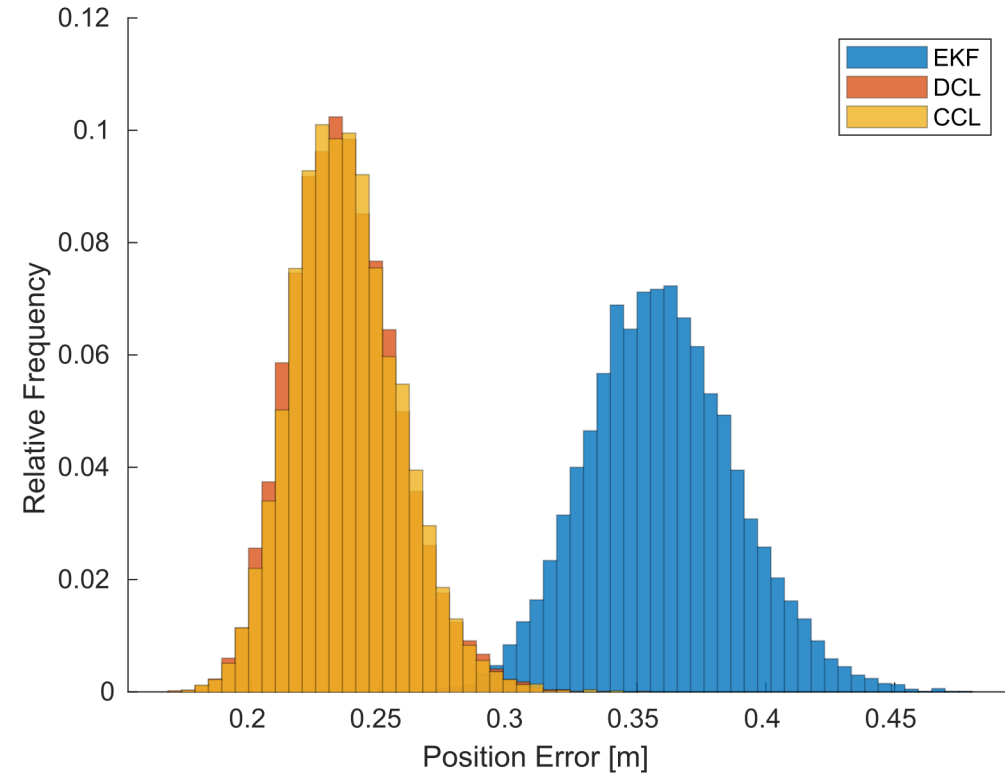
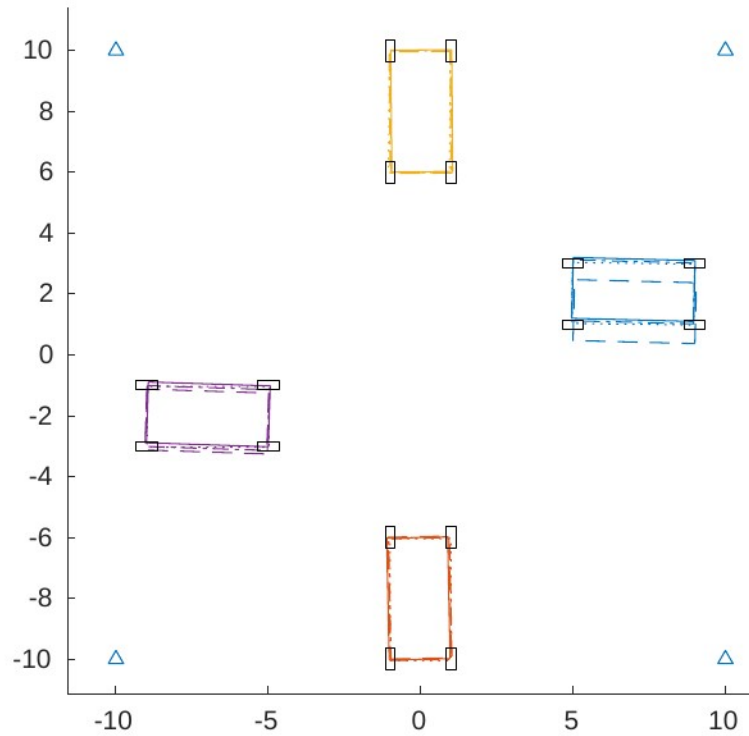
Simulation Results

- Parallel Motion



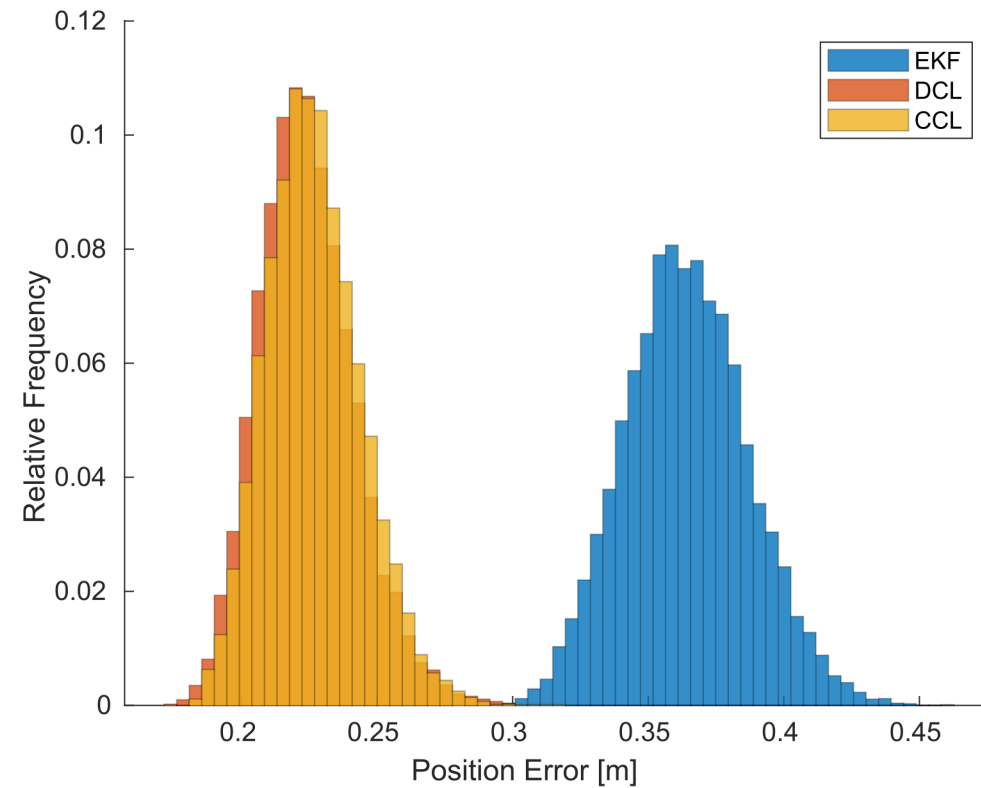
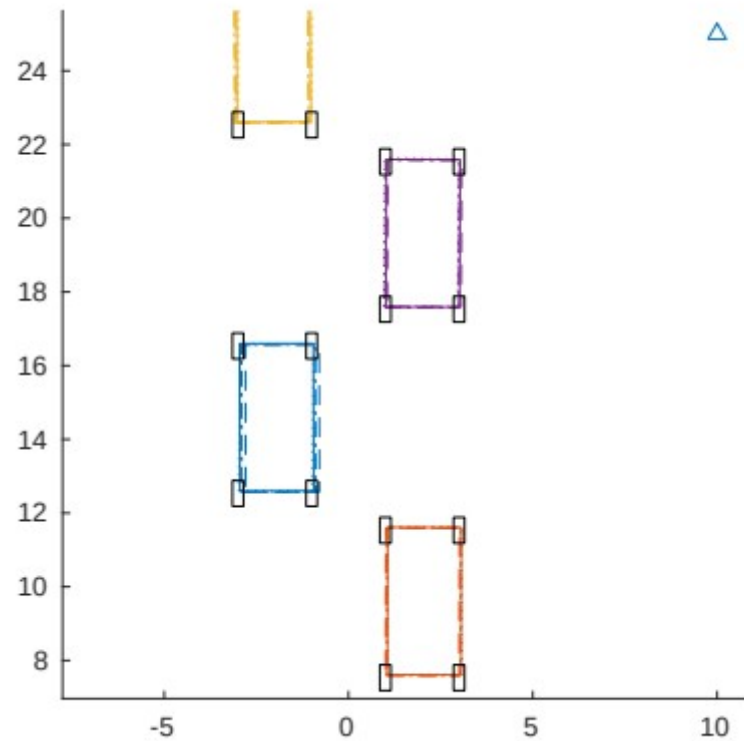
Simulation Results

- Street Crossing



Simulation Results

- Tunnel Environment – No GPS with Landmarks



Simulation Results Summary

- UWB offers improvements with collaboration
- Larger vehicle networks increased accuracy
- Greater improvements seen from landmarks
- Largest impact in GPS-denied settings

Experiment	GPS	EKF	DCL	CCL
Parallel	Yes	0.37	0.28	0.28
Street Crossing	Yes	0.37	0.24	0.24
Tunnel	No	0.30	0.24	0.24

Experimentation



Texas Transportation Institute, 2018, *Self-Driving Vehicles Begin Operating in Downtown Bryan, Texas* [17]

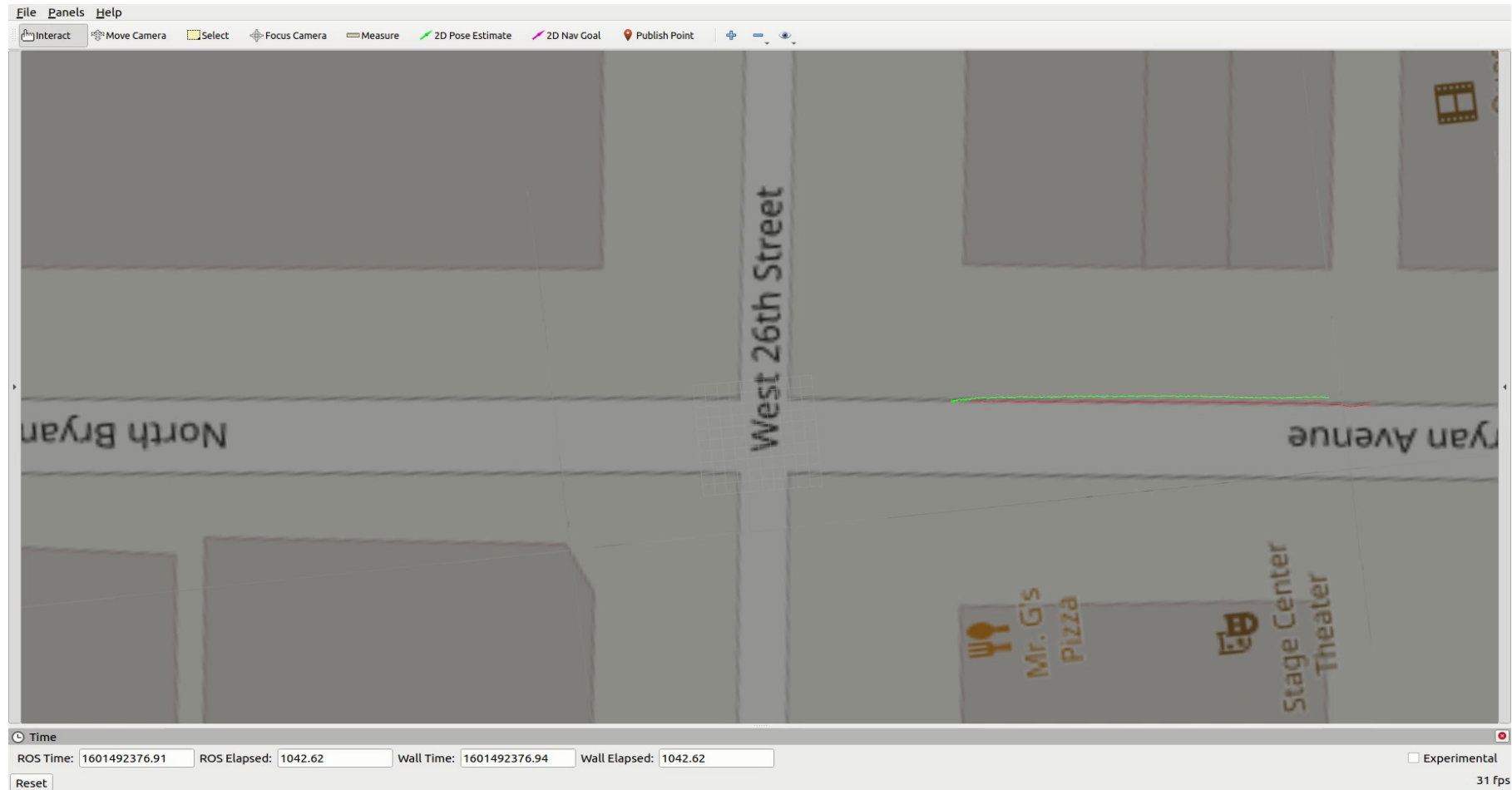
Experimental Setup

- Unmanned Lab Autonomous Trolley
- Sensors:
 - IMU
 - Odometry
 - GPS (RTK corrections available)
 - UWB Ranging – Collaborative and Landmarks
- Localization Algorithms:
 - EKF
 - EKF with UWB landmark ranging
 - DCL with UWB vehicle ranging

Experimental Data - Crossing



Experimental Data - Tunnel



Experimental Results Summary

- UWB offers improvements with collaboration
- Greater improvements seen from landmarks
- Largest impact in GPS-denied settings

Experiment	GNSS	EKF	DCL	CCL
Parallel	No	2.06	1.81	1.81
Street Crossing	Yes	2.32	1.61	1.61
Tunnel	No	7.78	1.30	1.30

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Contributions

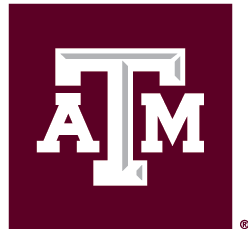
- Developed flexible collaborative simulation
 - Various scenes and vehicle parameters
 - Monte Carlo testing capability
- Decawave ROS driver package
- UWB error model validation
- Validations of Luft's DCL algorithm

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